

Problem

Prove that there does not exist a doubly-infinite sequence (x_k) of positive reals satisfying

$$2x_{k-1}x_{k+1} > x_{k-1}x_k + x_kx_{k+1}$$

for all $k \in \mathbb{Z}$.

(Math Problem of the Week, 6/8/97)
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